

# Index appearance record for transforming Rabin automata into parity automata

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Constructing correct-by-design systems from specifications given in linear temporal logic (LTL) is a classical problem [PR89], called *LTL synthesis*. The automata-theoretic solution to this problem is to translate the LTL formula to a deterministic automaton and solve the corresponding game on the automaton. Although different kinds of automata can be used, a reasonable choice is parity automata (DPA) due to the practical efficiency of parity game solvers [FL09,ML16] and the fact they allow for optimal memoryless strategies. Thus, the bottleneck of the automata-theoretic approach is to create a reasonably small DPA.

The classical way to transform LTL formulae into DPA is to first create a non-deterministic Büchi automaton (NBA) and then determinize it, as implemented in e.g. `ltl2dstar` [KB06]. Since determinization procedures [Pit06,Sch09] based on Safra’s construction [Saf88] are inefficient in practice, many alternative approaches to LTL synthesis arose. For example, some try to avoid determinization and/or focus on fragments of LTL, e.g. [KV05,PPS06,AL04].

Fortunately, new results on translating LTL directly and efficiently into deterministic automata [KE12,EK14] have been discovered recently. This opens new possibilities for the automata-theoretic approach. Indeed, tools such as Rabinizer [KK14] or LTL3DRA [BBKS13] can produce reasonably small deterministic Rabin automata (DRA) for complex formulae. Consequently, the task is to efficiently transform DRA into DPA, which is the aim of this paper.

Various kinds of deterministic automata can be transformed into deterministic parity automata by using variants of the traditional appearance-record construction. This construction intuitively introduces finite memory of recent, important events into the state space, which allows to formulate the acceptance condition. We present an efficient variant of this approach, specifically tailored to Rabin automata. Further, we introduce several optimizations applicable to all appearance records.

Experimental evaluation suggests an inherent advantage over exiting approaches solving the DRA to DPA translation. Moreover, the experiments demonstrate the potential of our method for LTL synthesis when combined with LTL-to-Rabin translators like Rabinizer. Especially, our “toolchain” leads to significantly smaller parity automata when compared to state-of-the-art approaches on various formulae.

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